

# OPTIMIZING LOG SUPPLY FROM TIMBER CONCESSION COMPLEX, DUNGUN, TERENGANU TO THEIR SUBSIDIARIES DOWN STREAM PROCESSING MILLS USING LINEAR PROGRAMMING MODEL ${ }^{\text {\# }}$ 

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#### Abstract

This paper attempts to solve the problem of irregular supply of logs to the mills within the same holding company. Linear programming model analysis has been used in solving this problem. The logs supply from concession area is not sufficient. Buying additional logs from other log yards to meet the demand by the mills is recommended. The study shows that the supplier company can increase its net income by RM 1.5 million (before tax) if the log supply to the mills by buying logs buying from other concession areas is improved to an efficient manner.


Key words: Optimization, net income, distribution, logs

## INTRODUCTION

Linear programming (LP) is mathematical techniques that are concerned with optimization, that is with finding the best possible answer to a problem. They are often associated with the wider field of operations research. They have been studied and researched since the late (Beasley, 1996). In the actual fact, LP is an aid to decision making in the field such as forestry, agricultural, industry, business and service sectors. It is a procedure that has found practical application in almost all kinds of business, from advertising to production planning. Transportation, distribution and aggregate production planning's are the most typical objectives of LP analysis. It is important for the reader to appreciate/understand at the outset that the programming in $L P$ is of a different meaning than the programming in 'computer programming'. In the former case it means to plan, while in the latter it means to write instructions for performing calculation.

As mentioned earlier, LP is a method of determining an optimum program of interdependent activities within available resources. The term linear assumes that all relationships involved in the particular problem to be solved by this method are linear. The term programming refers to the process of determining a particular program or plan of action. A linear programming arises whenever two or more activities compete for limited resources. According to Schrage (1986) linear programming is a mathematical procedure for determining optimal allocation of scarce resources. It is not only capable of allocating the resources in order to achieve optimal return but also capable of selecting the most profitable activities in the business operation. In agricultural project, LP model has been used as investment decision model in regional land evaluation for maximizing profit by utilizing the available resources (Ahmad Fauzi, 1994). In fact optimization planning is a refinement of conventional planning, which is emphasizes more on the solving of optimal plan to satisfy feasibility constraints (Loucks, 1985). This concept is applied under this study.

## PROBLEM OF THE STUDY

This study attempts to examine the problem of irregular log supply from Timber Concession Complex, Dungun, Terengganu to their processing subsidiary companies i.e. Syarikat PESAMA Timber Corporation Sdn Bhd, PESAKA Terengganu Berhad and PERMINT Plywood Sdn Bhd. These processing mills are subsidiary companies under the Golden Pharos Berhad, a public listed company. In fact the Timber

Complex's is responsible for supplying of raw logs to these mills. At the moment, Timber Concession Complex's could only managed to supply about $70 \%$ of the total logs requirement and each subsidiary company was requested to purchase the balance from outside Timber concession Complex. This study tries to determine how much profit could be achieved if all the logs supply is provided by The Timber Concession complex. Hence the mills could concentrated only on the down stream processing activities.

## THE SCOPE OF THE STUDY

This study was carried out at Timber Concession Complex, which is located at Bandar Bukit Besi, District of Dungun, Terengganu. in the east coast of Peninsular Malaysia. The total concession area own by Timber Concession Complex is about $108,900 \mathrm{ha}$; out of this area only 3,200 ha are allow to be logged per year. This study also used a secondary data obtained/derived from the Timber Concession Complex, Dungun, Terengganu and the processing mills to examine the problem of irregular log supply as well as the distribution of logs to the processing mills.

## THE OBJECTIVES OF THE STUDY

In general, the objective of this study was to determine the optimal logs distribution supply from Timber Concession Complex to the processing mills in order to optimize net return for one-year accounting period. The optimizing process would be considered by which Timber Concession Complex could produced logs within the existing limited annual coop allowed for harvesting in order to optimize the most efficient manner it's net return. The detailed working objectives of the study were as follows:
i) To estimate the expected net return of Timber Concession Complex for one-year period with and without purchase logs from outside concession areas in order to supply all the three mills;
ii) To compute the quantity of logs required to be purchased by Timber Concession Complex from other concession areas which for supplying the mills;
iii) To compute the additional cost required if Timber Concession Complex acts as the only supplier of logs to these three mills.

Other than that, this study would like to find out the volume of logs required according to grade need to be purchased from outside to meet the total requirement of all the three subsidiary processing mills.

## METHODOLOGY OF THE STUDY

This study used LP to optimize the log distribution from Timber Concession Complex to the mills and optimize the net return subject to the limited supply of logs. The amount of log supply is very much dependent on the predetermined quantity of demand by the processing mills. Generally, the LP model can be written as follows;

Maximize $\quad\{$ Net return\}
Subject to

> \{Supply constraints $\}$
> \{Input requirement/cost requirement per unit by grade $\}$
> $\{$ Demand constraints from the mills $\}$

This model ultimately would maximize the net return of Timber concession complex operation for one year with limited log supply. The model is also capable of to estimate the amount of logs required from other concession areas open market in order to meet the demand by the subsidiary mills by adding the buying component variables. This analysis will use Linear Integer and Quadratic Programming Program (LINDO) software.

## THE ASSUMPTIONS OF THE MODEL

LP is one of the most powerful economics tools in solving the optimization problem for planning over 30 years, but a number of assumptions are made (Hazell \& Norton 1986). They are listed as follows:
i) Optimization

The objective function is maximized or minimized. The above model maximizes the net return.
ii) Fixedness

Linear programming matrix is at least a one non-zero constraint for the right hand side coefficient.
iii) Finiteness

It is assumed that there are only a finite number of activities and constraints to be considered so that a solution may be sought.
iv) Determinism

All the coefficients used in the linear programming model matrix are assumed to be known constraints.
v) Continuity

Resources can be used and activities produced in quantities that are fractional units.
vi) Homogeneity

All units of the same resource or activity are identical.
vii) Additivity

The activities are assumed to be additive in the sense that when two or more are used, their total product is the sum of their individual products. That is, no interaction effect between activities are permitted; and
viii) Proportionality

The net farm income and resource requirement per unit of activity is assumed to be a constraint according to the mill requirement.
ix) Service Charges

Timber Concessionaire Complex will charge $8 \%$ for service charged on the logs selling price to the processing mills.

The addictively and proportionality together define linearity in the activities, thereby giving rise to the name linear programming.

## THE DATA FOR THE STUDY

This study was based on the data provided by Timber Concession Complex. The most important data to be acquired for the LP matrix is the cost per meter cubic. This is the basis of selecting logs to the appropriate mills for maximizing the net return. The buying and selling price of logs according to grade are next in importance variable for the study. LP should be able to select the low buying price and high selling price of log. Other than that, the constraints in the form of the quantity demand required by the mills according to grade also played an important role in determining the type(s) of logs to be purchased. The data used from this study are shown in the tables below.

Table 1: Average conventional logging cost per cubic meter ( $\mathrm{RM} / \mathrm{m}^{3}$ )

| ACTIVITIES | RM/m3 | $\%$ | Standard <br> Deviation |
| :--- | :---: | :---: | :---: |
| Premium | 23.63 | 16.73 | 8.78 |
| Pre-F inventory | 0.45 | 0.32 | 0.17 |
| Tree marking | 0.95 | 0.67 | 0.34 |
| Boundary delineation | 0.15 | 0.11 | 0.08 |
| Harvesting | 50.41 | 35.69 | 4.48 |
| Royalty \& silvicultural cess | 22.31 | 15.79 | 0 |
| Closing report | 0.38 | 0.27 | 0.15 |
| Post-F inventory | 0.6 | 0.42 | 0.21 |
| Forest treatment | 1.32 | 0.93 | 0.49 |
| Road and matau construction | 3.75 | 2.65 | 2.14 |
| Administration | 37.3 | 26.41 | 16.3 |
| Total | 141.25 | 100.00 |  |

Table 2: Average buying and selling price of logs per cubic meter $\left(\mathrm{RM} / \mathrm{m}^{3}\right)$

| Items\# | Buying price | Selling price |
| :--- | :---: | :---: |
| Grade 1 | 712 | 768.96 |
| Grade 2 | 502 | 543.24 |
| Grade 3 | 323 | 348.84 |

\# Grade 1 - Heavy hardwood, Grade 2 - Medium hardwood, Grade 3 - Mixed hardwood.
Table 3: Average quantity of logs (raw) required by mills per year $\left(\mathrm{m}^{3} / \mathrm{yr}\right)$

| Items | Pesama Timber <br> Corp Sdn Bhd | Pesaka <br> Terengganu Bhd | Permint <br> Plywood Sdn <br> Bhd | Total <br> $\left(\mathrm{m}^{3}\right)$ |
| :--- | :---: | :---: | :---: | :---: |
| Grade 1 | 17,500 | 18,000 |  | 35,5000 |
| Grade 2 | 8,750 | 9,000 | 30,000 | 47,750 |
| Grade 3 | 8,750 | 9,000 | 30,000 | 47,750 |
| Total | 35,000 | 36,000 | 60,000 | 131,000 |

Table 4: The quantity of logs available based on pre-F inventory per year $\left(\mathrm{m}^{3} / \mathrm{yr}\right)^{*}$

| Items | Quantity $\left(\mathrm{m}^{3} /\right.$ year $)$ |
| :--- | :---: |
| Grade 1 | 25,000 |
| Grade 2 | 40,000 |
| Grade 3 | 25,000 |
| Total | 90,000 |

* This is the capacity of Timber Concession Complex production per year. It is assumed that the rest of quantity required is bought from outside.


## THE ESTIMATED LINEAR PROGRAMMING MODEL

Based on the objectives of the study, which are to maximize the total net return, and at the same time to optimize the log distribution to the mill as requested by the processing mills. Considering the objectives and the data required, the estimated LP model is as shown below.

The Model:

```
MAX - 712 BUY_G1-503 BUY_G2 - 323 BUY_G3-141.25 KP1-141.25 KP2
    -141.25 KP3 + 686 PE1 + 518 PE2 + 308 PE3 + 686 BE1 + 518 BE2
    + 308 BE3 + 518 FY2 + 308 FY3 + 768.96 PE1B + 543.24 PE2B
    +348.84 PE3B + 768.96 BE1B + 543.24 BE2B + 348.84 BE3B
    + 543.24 FY2B + 348.84 FY3B
```


## SUBJECT TO

```
KP1 = 25000
KP2 = 40000
KP3 = 25000
23.63 KP1 + 23.63 KP2 + 23.63 KP3 >= 0
0.45 KP1 + 0.45 KP2 + 0.45 KP3 >= 0
0.95 KP1 + 0.95 KP2 + 0.95 KP3>=0
0.15 KP1 + 0.15 KP2 + 0.15 KP3 >= 0
50.41 KP1 + 50.41 KP2 + 50.41 KP3>= 0
22.31 KP1 + 22.31 KP2 + 22.31 KP3>= 0
0.38 KP1 + 0.38 KP2 + 0.38 KP3>= 0
0.6 KP1 + 0.6 KP2 + 0.6 KP3 >= 0
1.32 KP1 + 1.32 KP2 + 1.32 KP3>= 0
3.75 KP1 + 3.75 KP2 + 3.75 KP3>= 0
41.03 KP1 + 37.3 KP2 + 33.57 KP3>= 0
KP1-PE1-BE1 >= 0
KP2 - PE2 - BE2 - FY2 >= 0
KP3 - PE3 - BE3 - FY3 >= 0
BUY_G1 - PE1B - BE1B >= 0
BUY_G2 - PE2B - BE2B - FY2B >= 0
BUY_G3 - PE3B - BE3B - FY3B >= 0
PE1 + PE1B <= 17500
PE2 + PE2B <= 8750
PE3 + PE3B }<=875
BE1 + BE1B <= 18000
BE2+BE2B}<=900
BE3+ BE3B}<=900
FY2 + FY2B <= 30000
FY3 + FY3B <= 30000
-712 BUY_G1 + C_GRD_1 >= 0
-503 BUY_G2 + C_GRD_2>= 0
- 323 BUY_G3 + C_GRD_3 >}=
PE1 + PE2 + PE3 + PE1B + PE2B + PE3B = 35000
BE1 + BE2 + BE3 + BE1B + BE2B + BE3B = 36000
FY2 + FY3 + FY2B + FY3B = 60000
PE1 + BE1 = 25000
PE2 + BE2 + FY2 = 40000
PE3 + BE3 + FY3 = 25000
```

Table 5: Description of Variables.

| Variable name | Description |
| :--- | :--- |
| BUY_G1 | Buying grade 1 logs from outside KPKKT |
| BUY_G2 | Buying grade 2 logs from outside KPKKT |
| BUY_G3 | Buying grade 3 logs from outside KPKKT |
| KP1 | Log production grade 1 by Complex |
| KP2 | Log production grade 2 by Complex |
| KP3 | Log production grade 3 by Complex |
| PE1 | Selling grade 1 logs to PESAMA from Concession complex |
| PE1B | Selling grade 1 logs to PESAMA from outside Concession |
| PE2 | Selling grade 2 logs to PESAMA from Concession complex. |
| PE2B | Selling grade 2 logs to PESAMA from outside Concession |
| PE3 | Selling grade 3 logs to PESAMA from Concession complex |
| PE3B | Selling grade 3 logs to PESAMA from outside Concession |
| BE1 | Selling grade 1 logs to PESAKA from Concession complex |
| BE1B | Selling grade 1 logs to PESAKA from outside Concession complex. |
| BE2 | Selling grade 2 logs to PESAKA from Concession Complex. |
| BE2B | Selling grade 2 logs to PESAKA from outside Concession Complex |
| BE3 | Selling grade 3 logs to PESAKA from Concession Complex. |
| BE3B | Selling grade 3 logs to PESAKA from outside Concession complex) |
| FY1 | Selling grade 1 logs to PERMINT from Concession complex.. |
| FY1B | .Selling grade 1 logs to PERMINT from outside <br> complex |
| FY2 | Selling grade 2 logs to PERMINT from COMPLEX Concession |
| FY2B | Selling grade 2 logs to PERMINT from outside Complex Concession |
| FY3 | Selling grade 3 logs to PERMINT from KPKKT Concession |
| FY3B | Selling grade 3 logs to PERMINT from outside Complex Concession |

Note: Complex - Timber concession Complex..

## RESULTS AND DISCUSSION

a) The expected net farm income

From the analysis, Timber Concession Complex could get net return of about RM 32,857,500 if it only sells logs from her own concession area to her subsidiaries companies. However, if Timber Concession Complex acts as the sole log distributor for all the mills within the holding company, the net profit could be increased up to RM 34,355,300. An increased by RM $1,497,800$ per year as expected (Table 6). It is an increased by $4.6 \%$ of net return.
b) The quantity of logs required from outside by Grade.

Based on the previous Pre-F inventory record, Timber Concession Complex's has found that it can only supply about $90,000 \mathrm{~m}^{3}$ of logs per year. The first run of LP has managed to allocate the logs to the various mills and at the same time to maximize the net income. LP has allocated $7,000 \mathrm{~m}^{3}$ Grade 1 and $1,000 \mathrm{~m}^{3}$ Grade 2 logs to Pesama mill; $18,000 \mathrm{~m}^{3}$ Grade 1 and $9,000 \mathrm{~m}^{3}$ Grade 2 logs to Pesaka mill; and $30,000 \mathrm{~m}^{3}$ Grade 2 and $25,000 \mathrm{~m}^{3}$ Grade 3 logs to Permint mill (Table 6). However, the total requirement of logs for all the subsidiaries mills were estimated at $131,000 \mathrm{~m}^{3}$. The balance of logs required estimated $41,000 \mathrm{~m}^{3}$ must be purchased by Timber Concession Complex from open market and than resell back to the processing mills.

LP matrix has been developed in solving this problem. The result shows that Timber Concessions Complex is required to purchase adiditional $10,500 \mathrm{~m}^{3}$ Grade $1,7,750 \mathrm{~m}^{3}$ Grade 2 and $22,750 \mathrm{~m}^{3}$ Grade 3 logs in order to cope with the demand for all the subsidiaries mills at the market price.

Using LP, these quantity has been resell back $10,500 \mathrm{~m}^{3}$ Grade $1,7,750 \mathrm{~m}^{3}$ Grade 2 and $8,750 \mathrm{~m}^{3}$ Grade 3 to Pesama mill; $9,000 \mathrm{~m}^{3}$ Grade 3 to Pesaka; and $5,000 \mathrm{~m}^{3}$ Grade 3 to Permint mill (Table $6)$.

Table 6: The result of analysis if supply solely from Timber complex vs supply Timber Concessionaires Complex plus buying from out side

| Bil. | Items | Grade | Unit | Supply of Timber <br> Concessions <br> Complex Plus <br> Buying | Supply from <br> Timber <br> Concessions <br> Complex Only | Differences ( $+/-$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Purchasing) from <br> Outside |  |  |  |
| 1 | Net Farm Income |  | RM | $34,355,300$ | $32,857,500$ | $1,497,800$ |
|  |  |  |  |  |  |  |
|  | Log Supply |  |  |  |  |  |
| 2 | Pesama Sdn Bhd | 1 | $\mathrm{M}^{3}$ | 17,500 | 7,000 | 10,500 |
| 3 | Pesama Sdn Bhd | 2 | $\mathrm{M}^{3}$ | 8,750 | 1,000 | 7,750 |
| 4 | Pesama Sdn Bhd | 3 | $\mathrm{M}^{3}$ | 8,750 |  | 8,750 |
| 5 | Pesaka Sdn Bhd | 1 | $\mathrm{M}^{3}$ | 18,000 | 18,000 | 0 |
| 6 | Pesaka Sdn Bhd | 2 | $\mathrm{M}^{3}$ | 9,000 | 9,000 | 0 |
| 7 | Pesaka Sdn Bhd | 3 | $\mathrm{M}^{3}$ | 9,000 |  | 9,000 |
| 8 | Permint Plywood <br> Sdn Bhd | 2 | $\mathrm{M}^{3}$ | 30,000 | 30,000 | 0 |
| 9 | Permint Plywood <br> Sdn Bhd | 3 | $\mathrm{M}^{3}$ | 30,000 | 25,000 | 5,000 |
|  | Total |  |  | 131,000 | 90,000 | 41,000 |

c) The Additional funding required with and without buying logs from outside.

The result shows that the Timber Concession Complex requires RM 18,722,500 additional cost in order to purchase extra $41,000 \mathrm{~m}^{3}$ to met the requirement needed to all the subsidiaries mills. Out of these, the Timber Concession Compley, is required to allocate RM7,476,000 for Grade 1, RM3, 898,250 for Grade 2 and RM7,348,250 for Grade 3 logs (Table 7). Only under this condition when all these requirement are met, then all the mills would be able to run at the optimal level for the whole year and at the same time maximizing their net return.

Table 7: The additional funding required annually by the timber complex's to purchase the additional logs from open market

| No | Type of Logs | Quantity m3 | Price <br> RM $/ \mathrm{m} 3^{*}$ | Adsitional Cost (RM) |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Grade 1 | 10,500 | 712 | $7,4 \overline{76,000} 0$ |
| 2 | Grade 2 | 7,750 | 503 | $3,898,250$ |
| 3 | Grade 3 | 22,750 | 323 | $7,348,250$ |
|  | TOTAL | 41,000 |  | $18,722,500$ |

* Buying market price.


## CONCLUSION

LP applications is a very useful tools for solving optimization problems. This study emphases on maximizing the net income of the timber complex's in allocating the logs or raw materials from her concession area as well as from other sources to supply a sufficient raw logs to the fellow subsidiaries processing mills under the same holding company. LP shows also indicates that, The Timber Complex's could optimize the log distribution according to the mills' requirement with the main
objective to maximizing the net income. Based on the result of the study, The Timber Complex's can increase their net income by RM 1.5 million annually. Beside that, the study also indicates how logs can be distributed efficiently to all the mills according to grade and quantity specified.

## ACKNOWLEDGEMENTS

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A) LP OUTPUT WITHOUT BUYING LOGS FROM OUTSIDE KPKKT

LP OPTIMUM FOUND AT STEP 6
OBJECTIVE FUNCTION VALUE

1) 32857500.0

VARIABLE
KP1
KP2
KP3
PE1
PE2
PE3
BE1
BE2
BE3
FY2
FY3
C_GRD_1
C GRD 2 C_GRD_3

ROW
SUP ${ }^{-}$G2)
SUP_G3)
PREM)
PRE_F)
TREEMK)
BOND)
HARVT)
ROYSIL)
CLORPT)
POST_F)
FORTRET)
RDMT)
ADMIN)
SELL_G1)
SELL_G2)
SELL_G3)
S_G1PE)
S_G2PE)
S_G3PE)
S_G1BE)
$S$ G2BE)
S_G3BE)
S_G2PM) S_G3PM)
C_GRD1)
C GRD2)
C_GRD3)

VALUE
25000.000000
40000.000000
25000.000000
7000.000000
1000.000000
0.000000
18000.000000
9000.000000
0.000000
30000.000000
25000.000000
0.000000
0.000000
0.000000

SLACK OR SURPLUS
0.000000
0.000000
0.000000
2126700.000000 40500.000000 85500.000000
13500.000977
4536900.000000
2007900.000000
34200.000000
54000.003906
118800.007813
337500.000000
3357000.000000
0.000000
0.000000
0.000000
10500.000000
7750.000000
8750.000000
0.000000
0.000000
9000.000000
0.000000
5000.000000
$0.000000 \quad 0.000000$
$0.000000 \quad 0.000000$
$0.000000 \quad 0.000000$

RANGES IN, WHICH THE BASIS IS UNCHANGED:

| VARIABLE |  | OBJ COEFFICIENT | RANGES |
| :---: | :---: | :---: | :---: |
|  | CURRENT | ALLOWABLE | ALLOWABLE |
|  | COEF | INCREASE | DECREASE |
| KP1 | -141.250000 | INFINITY | INFINITY |
| KP2 | -141.250000 | INFINITY | INFINITY |
| KP3 | -141.250000 | INFINITY | INFINITY |
| PE1 | 686.000000 | 0.000000 | 686.000000 |
| PE2 | 518.000000 | 0.000000 | 518.000000 |
| PE3 | 308.000000 | 0.000000 | INFINITY |
| BE1 | 686.000000 | INFINITY | 0.000000 |
| BE2 | 518.000000 | INFINITY | 0.000000 |
| BE3 | 308.000000 | 0.000000 | INFINITY |
| FY2 | 518.000000 | INFINITY | 0.000000 |
| FY3 | 308.000000 | INFINITY | 0.000000 |
| C GRD_1 | 0.000000 | 0.000000 | INFINITY |
| C_GRD_-2 | 0.000000 | 0.000000 | INFINITY |
| C-GRD_3 | 0.000000 | 0.000000 | INFINITY |
| ROW | RIGHTHAND SIDE RANGES |  |  |
|  | CURRENT | ALLOWABLE | ALLOWABLE |
|  | RHS | INCREASE | DECREASE |
| SUP_G1 | 25000.000000 | 10500.000000 | 7000.000000 |
| SUP_G2 | 40000.000000 | 7750.000000 | 1000.000000 |
| SUP_G3 | 25000.000000 | 5000.000000 | 25000.000000 |
| PREM | 0.000000 | 2126700.000000 | INFINITY |
| PRE_F | 0.000000 | 40500.000000 | INFINITY |
| TREEMK | 0.000000 | 85500.000000 | INFINITY |
| BOND | 0.000000 | 13500.000977 | INFINITY |
| HARVT | 0.000000 | 4536900.000000 | INFINITY |
| ROYSIL | 0.000000 | 2007900.000000 | INFINITY |
| CLORPT | 0.000000 | 34200.000000 | INFINITY |
| POST_F | 0.000000 | 54000.003906 | INFINITY |
| FORTRET | 0.000000 | 118800.007813 | INFINITY |
| RDMT | 0.000000 | 337500.000000 | INFINITY |
| ADMIN | 0.000000 | 3357000.000000 | INFINITY |
| SELL_G1 | 0.000000 | 7000.000000 | 10500.000000 |
| SELL_G2 | 0.000000 | 1000.000000 | 7750.000000 |
| SELL_G3 | 0.000000 | 25000.000000 | 5000.000000 |
| S G1PE | 17500.000000 | INFINITY | 10500.000000 |
| S_G2PE | 8750.000000 | INFINITY | 7750.000000 |
| S_G3PE | 8750.000000 | INFINITY | 8750.000000 |
| S_G1BE | 18000.000000 | 7000.000000 | 1.0500 .000000 |
| S_G2BE | 9000.000000 | 1000.000000 | . 7750.000000 |
| S_G3BE | 9000.000000 | INFINITY | 9000.000000 |
| S_G2PM | 30000.000000 | 1000.000000 | 7750.000000 |
| S_G3PM | 30000.000000 | INFINITY | 5000.000000 |
| C_GRD1 | 0.000000 | 0.000000 | INFINITY |
| C_GRD2 | 0.000000 | 0.000000 | INFINITY |
| C-GRD3 | 0.000000 | 0.000000 | INFINITY |

B) LP OUPUT WITH BUYING LOGS FROM OUTSIDE KPKKT

LP OPTIMUM FOUND AT STEP

## OBJECTIVE FUNCTION VALUE

| 1) | 34355300.0 |  |
| :---: | :---: | :---: |
| VARIABLE | VALUE | REDUCED COST |
| BUY_G1 | 10500.000000 | 0.000000 |
| BUY_G2 | 7750.000000 | 0.000000 |
| BUY_G3 | 22750.000000 | 0.000000 |
| KP1 | 25000.000000 | 0.000000 |
| KP2 | 40000.000000 | 0.000000 |
| KP3 | 25000.000000 | 0.000000 |
| PE1 | 17500.000000 | 0.000000 |
| PE2 | 8750.000000 | 0.000000 |
| PE3 | 0.000000 | 0.000000 |
| BE1 | 7500.000000 | 0.000000 |
| BE2 | 9000.000000 | 0.000000 |
| BE3 | 0.000000 | 0.000000 |
| FY2 | 22250.000000 | 0.000000 |
| FY3 | 25000.000000 | 0.000000 |
| PE1B | 0.000000 | -0.000031 |
| PE2B | 0.000000 | 0.000000 |
| PE3B | 8750.000000 | 0.000000 |
| BE1B | 10500.000000 | 0.000000 |
| BE2B | 0.000000 | 0.000000 |
| BE3B | 9000.000000 | 0.000000 |
| FY2B | 7750.000000 | 0.000000 |
| FY3B | 5000.000000 | 0.000000 |
| C_GRD_1 | 7476000.000000 | 0.000000 |
| C_GRD_2 | 3898250.000000 | 0.000000 |
| C_GRD_3 | 7348250.000000 | 0.000000 |
| ROW | SLACK OR SURPLUS | DUAL PRICES |
| SUP_G1) | 0.000000 | -141.250000 |
| SUP_G2) | 0.000000 | -141.250000 |
| SUP_G3) | 0.000000 | -141.250000 |
| PREM) | 2126700.000000 | 0.000000 |
| PRE_F) | 40500.000000 | 0.000000 |
| TREEMK) | 85500.000000 | 0.000000 |
| BOND) | 13500.000977 | 0.000000 |
| HARVT) | 4536900.000000 | 0.000000 |
| ROYSIL) | 2007900.000000 | 0.000000 |
| CLORPT) | 34200.000000 | 0.000000 |
| POST_F) | 54000.003906 | 0.000000 |
| FORTRET) | 118800.007813 | 0.000000 |
| RDMT) | 337500.000000 | 0.000000 |
| ADMIN) | 3357000.000000 | 0.000000 |
| SELL_G1) | 0.000000 | 0.000000 |
| SELL_G2) | 0.000000 | 0.000000 |
| SELL_G3) | 0.000000 | 0.000000 |
| BUY_G1) | 0.000000 | -712.000000 |
| BUY_G2) | 0.000000 | -503.000000 |
| BUY_G3) | 0.000000 | $-323.000000$ |
| S_G1PE) | 0.000000 | : 31.119995 |
| S_G2PE) | 0.000000 | 14.399994 |
| S_G3PE) | $\therefore 0.000000$ | 0.000000 |
| S_G1BE) | 0.000000 | 31.120026 |
| S_G2BE) | 0.000000 | 14.399994 |
| S_G3BE) | 0.000000 | 0.000000 |
| S_G2 PM) | 0.000000 | 14.399994 |


| S_G3PM) | 0.000000 | 0.000000 |
| :--- | ---: | ---: |
| C_GRD1) | 0.000000 | 0.000000 |
| C_GRD2) | 0.000000 | 0.000000 |
| C_GRD3) | 0.000000 | 0.000000 |
| C_PE) | 0.000000 | 25.839996 |
| C_BE) | 0.000000 | 25.839996 |
| C_FY) | 0.000000 | 25.839996 |
| POL1) | 0.000000 | 629.040039 |
| POL2) | 0.000000 | 477.760010 |
| POL3) | 0.000000 | 282.160004 |

NO. ITERATIONS $=21$

RANGES IN WHICH THE BASIS IS UNCHANGED:

|  |  | OBJ COEFFICIENT RANGES |  |
| :---: | :---: | :---: | :---: |
| VARIABLE | CURRENT | ALLOWABLE | ALLOWABLE |
|  | COEF | INCREASE | DECREASE |
| BUY_G1 | -712.000000 | 712.000000 | 31.119995 |
| BUY_G2 | -503.000000 | 503.000000 | 14.399994 |
| BUY_G3 | -323.000000 | 14.399994 | INFINITY |
| KP1 | -141.250000 | INFINITY | INFINITY |
| KP2 | -141.250000 | INFINITY | INFINITY |
| KP3 | -141.250000 | INFINITY | INFINITY |
| PE1 | 686.000000 | INFINITY | -0.000031 |
| PE2 | 518.000000 | INFINITY | 0.000000 |
| PE3 | 308.000000 | 0.000000 | INFINITY |
| BE1 | 686.000000 | -0.000031 | INFINITY |
| BE2 | 518.000000 | INFINITY | 0.000000 |
| BE3 | 308.000000 | 0.000000 | INFINITY |
| FY2 | 518.000000 | 0.000000 | INFINITY |
| FY3 | 308.000000 | INFINITY | 0.000000 |
| PE1B | 768.960022 | -0.000031 | INFINITY |
| PE2B | 543.239990 | 0.000000 | INFINITY |
| PE3B | 348.839996 | 14.399994 | 0.000000 |
| BE1B | 768.960022 | INFINITY | -0.000031 |
| BE2B | 543.239990 | 0.000000 | INFINITY |
| BE3B | 348.839996 | 14.399994 | 0.000000 |
| FY2B | 543.239990 | INFINITY | 0.000000 |
| FY3B | 348.839996 | 0.000000 | INFINITY |
| C_GRD_1 | 0.000000 | 0.000000 | 0.043708 |
| C_GRD_2 | 0.000000 | 0.000000 | 0.028628 |
| $\mathrm{C}_{-} \mathrm{GRD}^{-}{ }^{3}$ | 0.000000 | 0.000000 | INFINITY |
|  |  | RIGHTHAND SIDE RANGES |  |
| ROW | CURRENT | ALLOWABLE | ALlowable |
|  | RHS | INCREASE | DECREASE |
| SUP_G1 | 25000.000000 | INFINITY | 0.000000 |
| SUP_G2 | 40000.000000 | INFINITY | 0.00000 c |
| SUP_G3 | 25000.000000 | INFINITY | 0.000000 |
| PREM | 0.000000 | 2126700.000000 | INFINITY |
| PRE_F | 0.000000 | 40500.000000 | INFINITY |
| TREEMK | 0.000000 | 85500.000000 | INFINITY |
| BOND | 0.000000 | 13500.000977 | INFINITY |
| HARVT | 0.000000 | 4536900.000000 | Infinity |
| ROYSIL | 0.000000 | 2007900.000000 | INFINITY |
| CLORPT | 0.000000 | 34200.000000 | INFINITY |
| POST_F | 0.000000 | 54000.003906 | INFINITY |
| FORTRET | 0.000000 | 118800.007813 | INFINITY |
| RDMT | 0.000000 | 337500.000000 | INFINIT |


| ADMIN | 0.000000 |
| ---: | ---: |
| SELL_G1 | 0.000000 |
| SELL_G2 | 0.000000 |
| SELL_G3 | 0.000000 |
| BUY_G1 | 0.000000 |
| BUY_G2 | 0.000000 |
| BUY_G3 | 0.000000 |
| S_G1PE | 17500.000000 |
| S_G2PE | 8750.000000 |
| S_G3PE | 8750.000000 |
| S_G1BE | 18000.000000 |
| S_G2BE | 9000.000000 |
| S_G3BE | 9000.000000 |
| S_G2PM | 30000.000000 |
| S_G3PM | 30000.000000 |
| C_GRD1 | 0.000000 |
| C_GRD2 | 0.000000 |
| C_GRD3 | 0.000000 |
| C_PE | 35000.000000 |
| C_BE | 36000.000000 |
| C_FY | 60000.000000 |
| POL1 | 25000.000000 |
| POL2 | 40000.000000 |
| POL3 | 25000.000000 |


| 3357000.000000 | INFINITY |
| ---: | ---: |
| 0.000000 | INFINITY |
| 0.000000 | INFINITY |
| 0.000000 | INFINITY |
| INFINITY | 10500.000000 |
| INFINITY | 7750.000000 |
| INFINITY | 22750.000000 |
| 7500.000000 | 0.000000 |
| 8750.000000 | 0.000000 |
| INFINITY | 0.000000 |
| 9000.000000 | 0.000000 |
| 9000.000000 | 0.000000 |
| INFINITY | 0.000000 |
| 5000.000000 | 0.000000 |
| INFINITY | 0.000000 |
| INFINITY | 7476000.000000 |
| INFINITY | 3898250.000000 |
| INFINITY | 7348250.000000 |
| 0.000000 | 8750.000000 |
| 0.000000 | 9000.000000 |
| 0.000000 | 5000.000000 |
| 0.000000 | 7500.000000 |
| 0.000000 | 22250.000000 |
| 0.000000 | 25000.000000 |

