

**THREE TERM CONJUGATE GRADIENT FOR  
SOLVING UNCONSTRAINED  
OPTIMIZATION**

**NUR FARAH HANIS BT ROZAIMI**

**Thesis Submitted in Fulfillment of the Requirement for  
Bachelor of Science (Hons.) Computational Mathematics in the  
Faculty of Computer and Mathematical Sciences  
Universiti Teknologi Mara**

**January 2018**

## DECLARATION BY CANDIDATE

I hereby declare that the thesis is based on my original work except for quotations and citations which have been duly acknowledged. I also declare that it has not been previously or concurrently submitted for any other degree at Universiti Teknologi MARA or other institutions.



---

NUR FARAH HANIS BT ROZAIMI

JANUARY 20, 2018

## ABSTRACT

Conjugate Gradient (CG) method is one of the popular methods that solve the large-scale unconstrained optimization problems, because they do not need the storage of matrices. In this paper, we are particularly interested in three-term conjugate gradient methods. We are using only classical parameter on this paper. In this paper, we are using exact line search. These methods have been tested using only the selected optimization test function with different initial point from the nearest to the solution point to the furthest from the solution point. The result is analysed based on the number of the iteration and CPU time. Based on the result, Narushima et al. is the best method of all in term of both number of iteration and CPU times.

**Keywords:** Conjugate Gradient (CG) Methods, Exact Line Searches, Global Convergence.

## TABLE OF CONTENTS

ABSTRACT	ii
ACKNOWLEDGEMENT	iii
DECLARATION BY THE SUPERVISOR	iv
DECLARATION BY THE CANDIDATE	v
TABLE OF CONTENTS	vi
LIST OF FIGURES	viii
LIST OF TABLES	x
LIST OF ABBREVIATIONS AND SYMBOLS	xi
Chapter 1: Introduction Of The Research	1
1.1 Introduction	1
1.2 Background Of Study	1
1.3 Problem Statement	5
1.4 Objectives	6
1.5 Significant Of Project	6
1.6 Scope Of The Project	7
1.7 Project Benefit	8
1.8 Definition Of Term And Concept	8
1.9 Literature Review	9
Chapter 2: Methodology	11
2.1 Introduction	11
2.2 Research Step	11
2.3 Fundamental of Conjugate Gradient Methods	18

2.3.1 Zhang et al. Method	18
2.3.2 Narushima et al. Method	18
2.3.3 Modified Three Term Hestenes-Steifel Method	19
2.3.4 Algorithms for all Method	19
2.4 Conclusion	23
Chapter 3: Implementation	24
3.1 Introduction	24
3.2 Calculation Example	24
3.3 Conclusion	29
Chapter 4: Results and Discussion	30
4.1 Introduction	30
4.2 Numerical Results	30
4.3 Discussion	41
4.4 Conclusion	49
Chapter 5: Conclusion	50
5.1 Introduction	50
5.2 Conclusion	50
5.3 Recommendation	51
REFERENCES	52
APPENDIX	55