

# First-Principles Study on Structural and Electronic Properties of Cubic (Pm3m) And Tetragonal (P4mm) ATiO<sub>3</sub> (A=Pb, Sn)

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## ABSTRACT

*This work focuses on exploring lead-free ferroelectric materials that have a comparable unique ns<sup>2</sup> solitary pair electrons with Pb (II), for example, Sn (II) using the first-principles study. All counts were performed dependent on ultrasoft pseudopotential of Density Functional Theory (DFT) that has been executed in the Cambridge Serial Total Energy Package (CASTEP). The convergence test for cut-off energy and k-point was performed to measure the accuracy of the calculations. It is shown that the structures have threshold energy of 350 eV and k-point of 4x4x4 with Monkhorst Pack. The structural properties for both cubic and tetragonal structures ATiO<sub>3</sub> (Pb, Sn) have shown the comparable value of the lattice parameter that was in agreement with previous work. Generalised gradient approximation (GGA) PBE displays the most exact qualities for cross-section parameters concerning exploratory qualities for both cubic PbTiO<sub>3</sub> while GGA-PBEsol functional is the best functional approximation for tetragonal PTO. The*



*electronic band structure and density of states show the presence of hybridizations between anion O 2p and cation Pb 6s/Sn 5s unique solitary pair in tetragonal PTO and SnTO stage. The calculations have shown that both cubic and tetragonal structure of ATiO<sub>3</sub> (A=Pb, Sn) has an indirect bandgap of 1.169 eV, 1.164 eV, 1.703 eV, and 1.016 eV respectively. It is shown that tetragonal structures have a higher value of bandgap compared to cubic structures.*

**Keywords:** *density functional theory; electronic properties; PbTiO<sub>3</sub>; SnTiO<sub>3</sub>*

## INTRODUCTION

Ferroelectrics are pyroelectric as they can initiate transitory voltage when they are warmed or cooled [1,2]. One of the best ferroelectric materials is perovskite oxide, which has a general chemical formula of ABO<sub>3</sub> [3]. Perovskite oxide will change its phase from tetragonal (P4mm) to cubic (Pm3m) at 800K [4,5]. Example of perovskites such as PbTiO<sub>3</sub> and SnTiO<sub>3</sub>. PbTiO<sub>3</sub> is widely used as piezoelectric sensors due to its high photorefractive sensitivity, memory, computer random-access memory (RAM), and radio-frequency identification (RFID) cards [6,7]. PbTiO<sub>3</sub> possess high spontaneous polarisation and dielectric constant of 0.75 C/m<sup>2</sup> and 1.767 x 10<sup>-2</sup> S/cm respectively [8]. However, since Pb is high in toxicity, it will increase air pollution and affect the environment [9]. A portion of the destructive impacts of Pb on a person can cause cerebral pain, a sleeping disorder, and cause forceful conduct [10]. It is profoundly required to supplant it with natural inviting and elite lead-free ferroelectric materials [11]. SnTiO<sub>3</sub> is anticipated to have a huge closeness with PbTiO<sub>3</sub> as Sn is in a similar group with Pb [12]. It also has higher spontaneous polarisation (1.1 C/m<sup>2</sup>) than Pb, indicating it as a good candidate to replace Pb [13]. Many researchers suggested SnTiO<sub>3</sub> is most likely suitable to reduce the consumption of Pb, creates a healthy and safe environment for the surrounding. Be that as it may, SnTiO<sub>3</sub> is not yet synthesis. A stable ferroelectric structure has been reported; however, there is no analysis of the electric polarisation [14]. Other than that, the strength of PbTiO<sub>3</sub> and SnTiO<sub>3</sub> are as yet vague [15]. It is hard to prepare a single period of SnTiO<sub>3</sub> due to the disproportional of Sn<sup>2+</sup> at high temperatures [16]. In this study, the structural and electronic properties of PbTiO<sub>3</sub> and SnTiO<sub>3</sub> are identified. Subsequently, the first-principles study

is used to investigate the electronic properties, phase stability, and strain properties of  $\text{PbTiO}_3$  and  $\text{SnTiO}_3$ . DFT can be dictated by computing the energy of the ground state, which comprises kinetic energy and potential energy [17].

## Computational Method

In this work, cubic (paraelectric,  $\text{Pm}3\text{m}$ ) and tetragonal (polar,  $\text{P}4\text{mm}$ )  $\text{ATiO}_3$  ( $\text{A}=\text{Pb}$ ,  $\text{Sn}$ ) were investigated by using DFT CASTEP computer code [18]. Convergence tests were carried out with convergence of energy change per atom  $<5 \times 10^{-6}$  eV, residual force  $<0.01$  eV/Å, stress  $<0.02$  GPa, and displacement of atoms  $<0.0005$  Å [19]. The k-point used for each compound of PTO and SnTO for both cubic and tetragonal structures was  $4 \times 4 \times 4$  with 350 eV cut-off energy Monkhorst Pack [20]. GGA-PBE and GGA-PBESol were utilised for cubic and tetragonal structures  $\text{ATiO}_3$  ( $\text{A}=\text{Pb}$ ,  $\text{Sn}$ ), respectively [21]. Consequently, it very well may be noticed that the extraordinary point connected for Brillouin zone cubic structure inspecting for all compounds ought to be set with a similar k-point ( $4 \times 4 \times 4$ ) in light of their comparative space group [22]. The electronic properties, which consist of band structure and density of state (DOS), were calculated by using ultrasoft pseudopotential [23].

## RESULTS AND DISCUSSION

### Geometrical Optimisation

Figure 1 shows the cubic and tetragonal structures for  $\text{ATiO}_3$ . The estimations of structural cross-section parameters for PTO and SnTO LDA, GGA-PBE, and GGA-PBESol functionals DFT are shown in Table 1 for cubic structure and Table 2 for tetragonal structure, respectively. The precision of the cross-section computation is significant because the difference in 1-2% of the grid will influence the unsteadiness of perovskite oxide. The test is fundamental to be completed to distinguish the best functional that would be implemented to different computations of new materials SnTO. The relative

deviations are overestimated 1.71% for LDA-CA-PZ, belittled 0.33% for GGA-PBE, and overestimated 0.78 % for GGA-PBESol when contrasted with the experiment of PTO (3.96 Å). The geometrical optimisation shows that GGA-PBE gives the best approximation with a percentage difference of less than 1%. Results, as organised in Table 2, show that each functional LDA-CAPZ and GGA-PBE for the tetragonal PTO gives more significant deviations in computing lattice parameter and volume. The lattice parameter utilising the GGA-PBESol is extremely near the experimental value, with just a deviation of 0.01%. This outcome is superior to anything than that of the determined outcomes utilising LDA-CAPZ and GGA-PBE with a deviation of +2.16% and -7.27%, respectively.

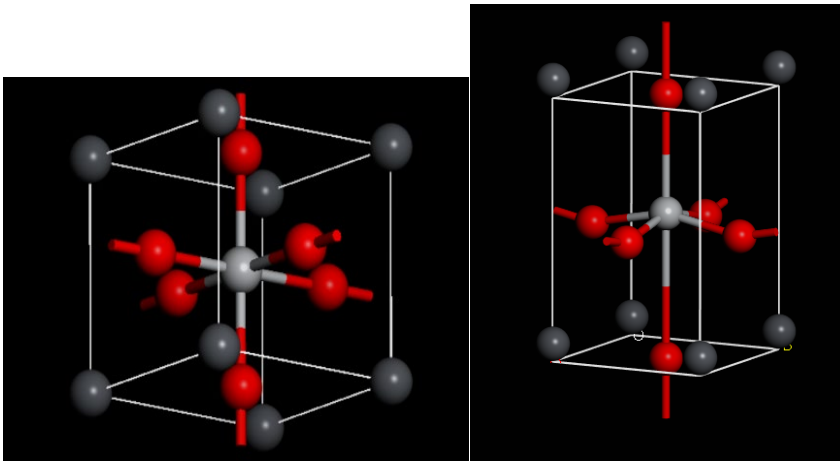


Figure 1: a) Cubic and b) Tetragonal structure of  $ATiO_3$  (A=Pb, Sn)

**Table 1: Lattice Parameter and Volume for Cubic ATiO<sub>3</sub> (A=Pb, Sn)**

ATiO <sub>3</sub>	Method	a (Å)	V (Å <sup>3</sup> )
<b>PbTiO<sub>3</sub></b>	LDA-CAPZ	3.892	58.9683
	GGA-PBE	3.973	62.7176
	GGA-PBEsol	3.929	60.6730
	Expt. [24]	3.960	62.0991
	Expt. [25]	4.049	66.3809
<b>SnTiO<sub>3</sub></b>	LDA-CAPZ	3.849	57.0611
	GGA-PBE	3.941	61.2004
	GGA-PBEsol	3.907	59.6346
	LDA-CAPZ [26]	3.850	57.0667
	GGA-PBE [27]	3.966	62.3818

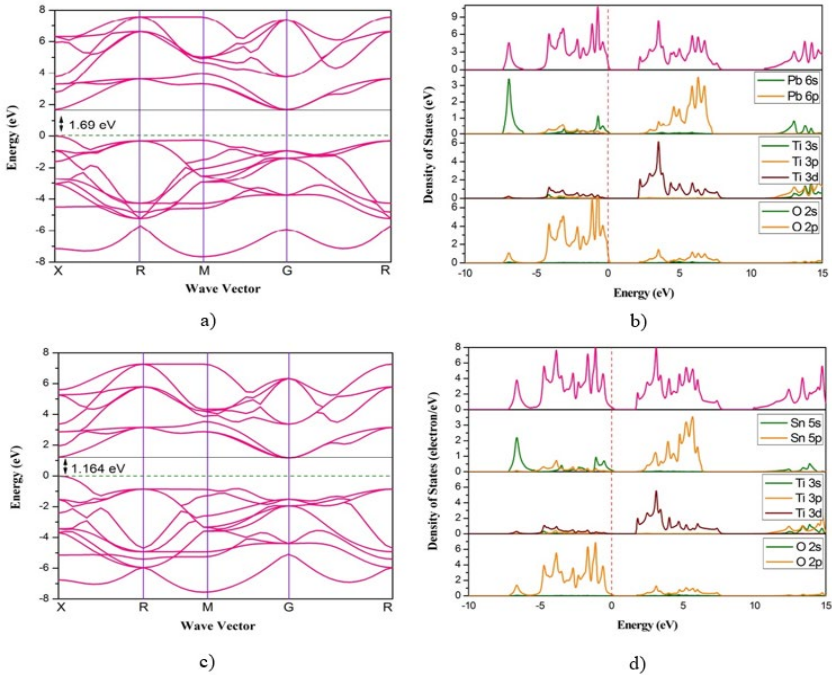
**Table 2: Lattice Parameter and Volume for Tetragonal ATiO<sub>3</sub> (A=Pb, Sn)**

ATiO <sub>3</sub>	Method	a (Å)	c (Å)	c/a	V (Å <sup>3</sup> )
<b>PbTiO<sub>3</sub></b>	LDA-CAPZ	3.873	4.010	1.04	60.1888
	GGA-PBE	3.842	4.801	1.25	70.9006
	GGA-PBEsol	3.889	4.169	1.07	63.0891
	Expt. [24]	3.890	4.167	1.07	63.0555
	LDA-CAPZ [28]	3.860	3.840	0.99	57.2145
<b>SnTiO<sub>3</sub></b>	LDA-CAPZ	3.743	4.352	1.16	60.9917
	GGA-PBE	3.820	4.734	1.24	69.1056
	GGA-PBEsol	3.808	4.459	1.17	64.6546
	LDA-CAPZ [29]	3.800	4.090	1.08	59.0596
	PWPP [30]	3.812	3.800	0.99	55.2191

## Band Structures and Density of States (DOS) of PTO and SnTO

The calculated electronic band structures of cubic PTO and SnTO at position of X (0.5, 0.0, 0.0), R (0.5, 0.5, 0.5), M (0.5, 0.5, 0.0) and G (0.0, 0.0, 0.0) using the GGA-PBE functional approximation in the Brillouin Zone is shown in Figure 2. For both PTO and SnTO, the most elevated valence band (VB) is ruled by the O-2p at X point, where it lies at the Fermi level. The most minimal conduction band (CB) is fundamentally overwhelmed by Ti-3d overlap with Pb-6p state at G-point. Five valence groups are mostly from the hybridisation of O-2p and Ti-3d orbitals beneath the Fermi level. These bands are very close and mixed. As calculated by using GGA-PBE functional, at X-G point, PTO has an indirect bandgap of 1.69 eV. In SnTO, the most astounding valence band (VB), which lies at the Fermi level ( $E_F$ ), is commanded by the O 2p at X point that comparable with the PTO compound. The CB for SnTO happens at G point, which is fundamentally ruled by Ti 3d blended occupied together with Sn p-state. SnTO has an indirect bandgap of 1.64 eV, which is smaller 0.05 compared to PTO. This value is in agreement with the experimental data, which has an indirect bandgap of 2.361 eV by applying a 1.4 eV scissor operator [31]. It is emphatically foreseen that the SnTO could be a great possibility to be doped in any Pb compound because of their similitude in special lone pair  $ns^2$  ( $n=5$  for Sn and  $n=6$  for Pb).

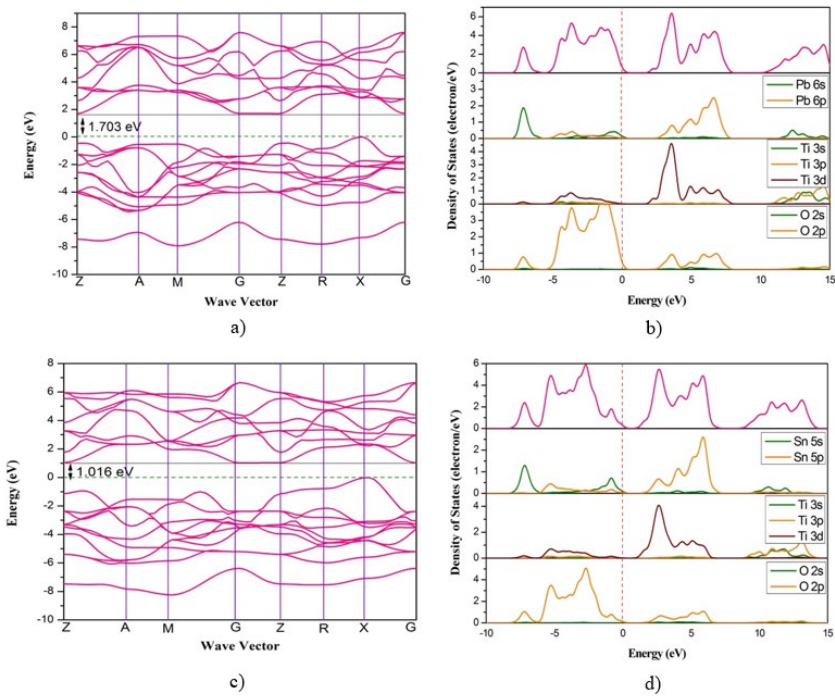
Electron dispersion in a vitality range could be portrayed by the density of state (DOS). Based on Figure 2, for the cubic structure, it indicates the CB area, which comprises predominantly of Ti 3d and Pb 6p nuclear orbitals with little commitments of O 2p and 2s states. The peak at Ti 3d shows a more grounded hybridisation between O 2p and Ti 3d when contrasted with O 2p and Pb 6s. As for SnTO, it can be seen that the VB of SnTO is just involved by electron O 2p and Sn 5s state. CB of SnTO is commanded by O 2p states that uncovered the presence of covalence association between cation Sn 5s (extraordinary solitary pair) and Ti 3d with O 2p states.



**Figure 2: a) Bandgaps and b) DOS of Cubic PbTiO<sub>3</sub> and c) Bandgaps and d) DOS of Cubic SnTiO<sub>3</sub>**

Figure 3 displays the determined electronic band structures for tetragonal structures along the lines Z-A-M-G-Z-R-X-G at the high-symmetry Brillouin zone of PTO and SnTO. The Fermi level is set to be at 0 eV, and it shows that the most elevated valence band (VB) is commanded by the O 2p at X point for both PTO and SnTO while the conduction band (CB) Ti 3d and A-p state (A=Pb, Sn) fundamentally rule for PTO and SnTO happen at G point. It portrays the indirect bandgap of PTO is 1.703 eV at X-G point. As for SnTO, the least value calculation of the indirect bandgap is 1.164 eV an incentive for SnTO is lower contrasted than that of past research on the cubic stage SnTO with a bandgap of 1.64 eV. Nonetheless, the bandgap of tetragonal PTO (1.703 eV) is slightly higher than cubic PTO (1.69 eV) with a percentage deviation of 0.76%. For tetragonal material comprises of the ATiO<sub>3</sub> framework, a solid covalent bonding happens between Ti-O and that nature bonding is additionally established in PTO and SnTO as displayed in DOS.

Furthermore, high covalent bonding is produced between Pb-O and Sn-O when the cation with exceptional lone pair  $ns^2$  states hybridised with the O 2p state. Be that as it may, the most noteworthy valence band (VB) in all materials, which lies at the Fermi level (EF), is principally credited to the O 2p states. While the conduction band (CB) is fundamentally overwhelmed by Ti 3d hybridise with the A (Pb, Sn) p-state for PTO and SnTO at the G point. This shows the strong covalent character displayed by A-O and Ti-O from the hybridisations between the lone pair ( $ns^2$ ) with O 2p and Ti-3d with O 2p individually.



**Figure 3: a) Band Gaps and b) DOS of Tetragonal PbTiO<sub>3</sub> and c) Band Gaps and d) DOS of Tetragonal SnTiO<sub>3</sub>**



## CONCLUSION

In conclusion, the best functionality for the cubic structure is GGA-PBE, while GGA-PBEsol for the tetragonal PTO and SnTO, respectively. The electronic band structure for cubic SnTiO<sub>3</sub> is like PbTiO<sub>3</sub>, which occurs at X-G point with a value of 1.164 eV and 1.69 eV, respectively. In any case, for the tetragonal structure of PbTiO<sub>3</sub> and SnTiO<sub>3</sub> demonstrates the bandgap at X-G point along the Brillouin zone with 1.703 eV and 1.016 eV individually. These outcomes are sensible and satisfactory, utilising an adjustment factor of 1.4 eV. The hybridisation of uncommon solitary pair ( $ns^2$ ) with O 2p and hybridisation of Ti 3d with O 2p inferring solid covalent bonds were made.

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