UNIVERSITI TEKNOLOGI MARA

TECHNICAL REPORT

A COMPARATIVE STUDY OF LEAST SQUARE METHOD, EXPONENTIAL SMOOTHING METHOD AND MOVING AVERAGE TO PREDICT FUTURE SALES OF PHARMACY

SITI NAJIHAH BINTI MD AJEMAN (2019422894) QASHRINA BALQIS BINTI JAMIL (2019405798)

FATIN NURUL IZZAH BINTI AHMAD HASBULLAH (2019415338)

(P48M22)

Report submitted in partial fulfillment of the requirement for the degree of Bachelor of Science (Hons.) (Mathematics)

Faculty of Computer and Mathematical Sciences

AUGUST 2022

ACKNOWLEDGEMENTS

First and foremost, we thank ALLAH S.W.T., the Almighty, for his guidance, mercy, and blessings in providing us with the strength to finish this task successfully. Even though we encountered some challenges, we were able to complete it on time.

We had to enlist the assistance and guidance of a few well-respected individuals in order to complete our task, and we owe them our deepest appreciation. We are quite pleased with the outcome of this job. We would also like to thank our supervisor Puan Rahmah Binti Shahril for giving opinions and monitoring every week to ensure the final year of the project there is improvement from time to time.

Without the effort and cooperation of our group members, we will be unable to finish this job. With our entire devotion and responsibility, we always strive hard to create a decent study.

Finally, we would like to express our gratitude to our parents for always assisting us when we needed it and supporting us psychologically and physically not just during this work but throughout this semester's academics. We appreciate everyone's assistance in completing our work, both directly and indirectly.

TABLE OF CONTENT

ACKNOWLEDGEMENTS	i
LIST OF TABLES	. iii
LIST OF FIGURES	. iii
ABSTRACT	
CHAPTER 1: INTRODUCTION	1
1.1 Introduction	1
1.2 Problem Statement	
1.3 Objectives	4
1.4 Scope and Limitation of Study	4
1.5 Significant and Benefit of Study	
1.6 Definition of Terms	
CHAPTER 2: BACKGROUND THEORY AND LITERATURE REVIEW	8
2.1 Mathematical Formula	
2.1.1 Least Square Method	8
2.1.2 Exponential Smoothing Method	9
2.1.3 Moving Average	10
2.2 Literature Review/ Related Research	
CHAPTER 3: METHODOLOGY AND IMPLEMENTATION	15
3.1. Research Process	
3.2. Problem Identification	
3.3. Data Description	16
3.4. Model Identification	
3.4.1 Regression Model	17
3.4.2 Exponential Smoothing Model	18
3.4.3 Moving Average Model	18
3.5 Implementation	
3.5.1 Calculation of LSM	
3.5.2 Calculation of ESM	
3.5.3 Calculation of MA	
3.6. Error Calculation between RMSE and MAPE	
CHAPTER 4: RESULTS AND DISCUSSION	35
4.1 Result of Least Square Method	35
4.2 Result of Exponential Smoothing Method	39
4.3 Result of Moving Average	
4.4 Error Comparison between LSM, ESM and MA	
4.5 Sales Forecasting of Pharmacy data	
CHAPTER 5: CONCLUSION AND RECOMMENDATION	
REFERENCES	
APPENDIX	

LIST OF TABLES

Table 1.2: Continued the list definition of terms7Table 2.1: MAPE value for prediction evaluation12Table 3.1: Data of total sales from 2000 to 202116Table 3.2: Summation value for LSM calculation19Table 3.3: Summation value for exponential function calculation23Table 3.4: Calculation for Single Exponential Smoothing24Table 3.5: Calculation for Double Exponential Smoothing26Table 3.6: Calculation for Simple Moving Average28Table 3.7: Calculation for Exponential Moving Average30Table 3.8: Calculation for Weighted Moving Average32Table 3.9: Error calculation34Table 4.1: Exact value and forecast value in 201538Table 4.2: Comparison error for Least Square Method45Table 4.3: Comparison error for Exponential Smoothing Method45Table 4.4: Comparison error for Moving Average46Table 4.5: Comparison error between Quartic, DES and EMA47Table 4.6: Predict sales of pharmacy from 2022 to 202648	Table 1.1: The list definition of terms	6
Table 2.1: MAPE value for prediction evaluation 12 Table 3.1: Data of total sales from 2000 to 2021 16 Table 3.2: Summation value for LSM calculation 19 Table 3.3: Summation value for exponential function calculation 23 Table 3.4: Calculation for Single Exponential Smoothing 24 Table 3.5: Calculation for Double Exponential Smoothing 26 Table 3.6: Calculation for Simple Moving Average 28 Table 3.7: Calculation for Exponential Moving Average 30 Table 3.8: Calculation for Weighted Moving Average 32 Table 3.9: Error calculation 34 Table 3.9: Error calculation 34 Table 4.1: Exact value and forecast value in 2015 38 Table 4.2: Comparison error for Least Square Method 45 Table 4.3: Comparison error for Exponential Smoothing Method 45 Table 4.4: Comparison error for Moving Average 46 Table 4.5: Comparison error between Quartic, DES and EMA 47 Table 4.6: Predict sales of pharmacy from 2022 to 2026 48 LIST OF FIGURES Figure 4.1: Graph of quadratic function 35 Figure 4.2: Graph of quadratic function 36 Figure 4.3: Graph of cubic function		
Table 3.1: Data of total sales from 2000 to 2021		
Table 3.2: Summation value for LSM calculation		
Table 3.3: Summation value for exponential function calculation		
Table 3.4: Calculation for Single Exponential Smoothing		
Table 3.5: Calculation for Double Exponential Smoothing	±	
Table 3.6: Calculation for Simple Moving Average		
Table 3.8: Calculation for Weighted Moving Average		
Table 3.9: Error calculation		
Table 4.1: Exact value and forecast value in 2015	Table 3.8: Calculation for Weighted Moving Average	32
Table 4.2: Comparison error for Least Square Method	Table 3.9: Error calculation	34
Table 4.3: Comparison error for Exponential Smoothing Method	Table 4.1: Exact value and forecast value in 2015	38
Table 4.4: Comparison error for Moving Average	Table 4.2: Comparison error for Least Square Method	45
Table 4.5: Comparison error between Quartic, DES and EMA	Table 4.3: Comparison error for Exponential Smoothing Method	45
Table 4.6: Predict sales of pharmacy from 2022 to 2026	Table 4.4: Comparison error for Moving Average	46
Table 4.6: Predict sales of pharmacy from 2022 to 2026	Table 4.5: Comparison error between Quartic, DES and EMA	47
Figure 3.1: Research Framework		
Figure 3.1: Research Framework		
Figure 4.1: Graph of linear function35Figure 4.2: Graph of quadratic function35Figure 4.3: Graph of cubic function36Figure 4.4: Graph of quartic function36Figure 4.5: Graph of exponential function37Figure 4.6: Graph of the different alpha39Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44	LIST OF FIGURES	
Figure 4.1: Graph of linear function35Figure 4.2: Graph of quadratic function35Figure 4.3: Graph of cubic function36Figure 4.4: Graph of quartic function36Figure 4.5: Graph of exponential function37Figure 4.6: Graph of the different alpha39Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44	E	1.5
Figure 4.2: Graph of quadratic function35Figure 4.3: Graph of cubic function36Figure 4.4: Graph of quartic function36Figure 4.5: Graph of exponential function37Figure 4.6: Graph of the different alpha39Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44		
Figure 4.3: Graph of cubic function36Figure 4.4: Graph of quartic function36Figure 4.5: Graph of exponential function37Figure 4.6: Graph of the different alpha39Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44		
Figure 4.4: Graph of quartic function		
Figure 4.5: Graph of exponential function37Figure 4.6: Graph of the different alpha39Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44		
Figure 4.6: Graph of the different alpha39Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44		
Figure 4.7: Graph of Single Exponential Smoothing39Figure 4.8: Graph of Double Exponential Smoothing40Figure 4.9: Graph of the different Years Simple Moving Average41Figure 4.10: Graph of the different Years Exponential Moving Average42Figure 4.11: Graph of the different Years Weighted Moving Average43Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average44		
Figure 4.8: Graph of Double Exponential Smoothing		
Figure 4.9: Graph of the different Years Simple Moving Average		
Figure 4.10: Graph of the different Years Exponential Moving Average		
Figure 4.11: Graph of the different Years Weighted Moving Average		
Figure 4.12: Graph of the different Weights for 2 Yearly Weighted Moving Average		

ABSTRACT

The Least Square Method (LSM) is widely utilized in data fitting, with the best fit minimizing the residual squared sum and can be used to forecast pharmacies sales. LSM can be divided into two categories, linear LSM and nonlinear LSM. Apart from LSM, Exponential Smoothing (ESM) and Moving Average (MA) are also used for forecasting. ESM is a time series forecasting method for univariate data that can be extended to support data with a systematic trend or seasonal component while MA is a statistical method used for forecasting long-term trends. These methods are only accurate when there is a reasonable amount of continuity between the past and the future. This study is to determine a model that fits the pharmacy data using LSM, ESM and MA. This study will compare which method is preferable by comparing their error using Root Mean Square Error (RMSE) and Mean Absolute Percentage Error (MAPE). We can predict the future sales of pharmacy for the next 5 years (2022-2026) using the preferable method. From the results of the study, the function that is obtained from LSM is quartic which is the best fit. It can be concluded that prediction analysis by using quartic can be used to predict the sales for the coming period based on the pharmacies data in the previous years, because it produces the smallest error. It can show that the pharmacies sales are decreasing after the pandemic Covid-19 because due to a price war between other pharmacies offering cheaper prices. The recommendation for the next study is to use Box-Jenkins based ARIMA model, Euler Method and Runge-Kutta to make prediction of pharmacies sales. Not only that, but it is also better to use larger data to make the curve fitting smoother for forecasting.