## MATHEMATICS

 I N A P P L I E D R E S E A R C HRECENT MATHEMATICAL PROJECTS AT UITM, SEREMBAN CAMPUS
Vol. 003


## Dispersion Relation Equation of Shallow Wate

## Solution of Fisher's Equation Using Integral Iterative Method



Applications of Institutionistic Fuzzy Analytic Hierarchy Process

## M A T H E M A T I C S I N A P P L I E D R E S E A R C H

BULETIN RASMI
KOLEJ PENGAJIAN PENGKOMPUTERAN, INFORMATIK, DAN MEDIA, UITM CAWANGAN NEGERI SEMBILAN KAMPUS SEREMBAN EDISI NOVEMBER 2022

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Semenjak tahun 2014, mahasiswa tahun akhir KPPIM (sebelumnya dikenali FSKM) Seremban telah menghasilkan banyak penyelidikan yang berpotensi untuk diketengahkan dalam dunia akademik. Akan tetapi tidak banyak yang berjaya diterbitkan dalam jurnal atau pun prosiding konferensi akademik kerana halangan tertentu seperti kualiti penyelidikan dan penulisan ilmiah. Oleh itu, penerbitan makalah ini diharapkan dapat menambahkan lagi ruang bagi penerbitan hasil penyelidikan warga KPPIM Seremban
Disamping itu, pihak KPPIM Seremban mengharapkan makalah ini akan menjadi rujukan dan pemangkin kepada usaha menghasilkan penyelidikan Projek Tahun Akhir yang lebih bermutu tinggi. Makalah ini juga adalah batu asas kepada perkongsian penyelidikan terkini daripada pelajar dan pensyarah KPPIM Seremban.
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semoga kecemerlangan perkhidmatan yang ditunjukkan oleh kedua editor-editor ini akan menjadi pendorong kepada editorial board yang seterusnya. Sekian. Terima kasih.


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# MATHEMATICS IN APPLIED RESEARCH 

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# MIXED INTEGER PROGRAMMING APPROACH FOR MINIMIZING TRAIN DELAY 

Nurul Liyana Abdul Aziz*, Nur Faqihah Jalil, Faridatul Azra Md Shamsul and Zaliyah Abbas<br>Faculty of Computer and Mathematical Sciences, Universiti Teknologi MARA (UiTM) Cawangan Negeri Sembilan, Kampus Seremban, Persiaran Seremban Tiga/1, 70300 Seremban, Negeri Sembilan.<br>*Corresponding author: liyana511@uitm.edu.my

Keywords: schedule, train, mixed integer programming

## 1. Introduction

In the high technological world of today, transportation maintains up with the advancement of human existence and culture. Additionally, it has improved economic structure by speeding up the distribution of economic growth. Malaysia is another nation that offers commuter rail services. The only provider of train commuter services in Malaysia is Keretapi Tanah Melayu, which offers services in the Klang Valley, Penang, Perak, and Johor. Railway service that is readily accessible to the general public is perfect for reducing highway traffic, especially in congested areas, and promoting environmentally responsible and sustainable growth. Malaysians prefer taking the train over driving because it saves them money while avoiding traffic and allows them to reach their destination on time. However, because of the technical fault could impair the railway network, the railway firm frequently encounters unforeseen issues, such as sudden changes to the original schedule (Alwadood et al., 2015).

This study is related to public scheduling problems and focuses on train scheduling problem. The aim of this study is to estimate the delay time from Padang Besar to Sungai Petani by using mixed integer programming. The train scheduling problem will be modelled as mixed integer programming and the data will be taken from the KTM Berhad website. By using Microsoft Excel, the model was used to estimate the delay time. At the end of this study, a new train schedules was proposed.

## 2. Methodology

This study explains the method and formulation of the train schedule using the mixed integer programming model to minimize the train delay by rescheduling the present timetable of KTM Berhad at station Padang Besar to Sungai Petani. Several essential steps are conducted during the study to achieve the result discussed in the following subsections.

At many stations, certain trains arrive or depart with delayed services, which is known as a call delay. The impact of a train delay is larger for passengers. Since each train precisely left from Padang Besar to Sungai Petani, the goal of this study is to determine the entire delay time of each train at several stations involved. The exact time of the train left is used to calculate the delay time.

The MIP model formulation is as follows:

To minimize

$$
\begin{equation*}
\sum_{p \in T} Z_{v_{p}} \tag{1}
\end{equation*}
$$

The objective function (1) is to calculate the minimum sum of delay experienced by all trains when it reaches their final destination.

Subject to

$$
\begin{equation*}
y_{r}^{I} \geq x_{r}^{I}+\Delta_{r}, r \in \mathrm{E} \tag{2}
\end{equation*}
$$

Constraints (2) describe the minimum running time for each of the train event.

$$
\begin{equation*}
y_{r}^{I} \geq x_{r+1}^{I}, r \in R_{p}, p \in T: k \neq v_{p} \tag{3}
\end{equation*}
$$

Constraints (3) shows that each train event must departed and arrive as the original schedule so that the next train could departed as scheduled.

$$
\begin{equation*}
y_{r}^{I} \geq x_{r}^{I}+\Delta_{r}, r \in E \tag{4}
\end{equation*}
$$

Meanwhile constraints (4) indicate that train need to depart and arrive as the scheduled time.

$$
\begin{equation*}
x_{r}^{I} \geq x_{r}^{S}, r \in E \tag{5}
\end{equation*}
$$

Constraints (5) represent the reschedule departure time should not be earlier than the scheduled departure time.

$$
\begin{equation*}
x_{r}^{I} \geq x_{r}^{A}, r \in E: x_{r}^{S}>0 \tag{6}
\end{equation*}
$$

Constraints (6) shows that departure time must depart as being schedule even though there might be a distraction.

$$
\begin{equation*}
y_{r}^{I} \geq y_{r}^{A}, r \in E: x_{r}^{S}>0 \tag{7}
\end{equation*}
$$

Constraints (7) indicates that arrival time must depart as being schedule even though there might be a distraction.

$$
\begin{equation*}
y_{r}^{I}-y_{r}^{S} \leq z_{r}, r \in E \tag{8}
\end{equation*}
$$

Constraints (8) define total delay of trains as the divergence in between reschedule and original schedule arrival times.

$$
\begin{equation*}
T_{i}=y_{r}^{A}-x_{r}^{A} \tag{9}
\end{equation*}
$$

Constraints (9) describe about the real travel time of train after arrived at the final destination.

## 3. Results and Discussions

To analyse the compatibility and ability of the model developed in the previous part, the model was further tested on a real KTMB train schedule. Table 1 contains seven different trains departed from Padang Besar to Sungai Petani with a different departure time. This data was taken from KTM Berhad website. The origin station is Padang Besar while the end station is Sungai Petani.

Table 1: Train schedule from KTM Berhad website

|  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| STATION | 2955 | 2959 | 2963 | 2965 | 2969 | 2971 | 2975 |
| Padang Besar | $12: 35$ | $14: 35$ | $16: 35$ | $17: 35$ | $18: 35$ | $19: 35$ | $21: 35$ |
| Bukit Ketri | $12: 47$ | $14: 47$ | $16: 47$ | $17: 47$ | $18: 47$ | $19: 47$ | $21: 47$ |
| Arau | $12: 54$ | $14: 54$ | $16: 54$ | $17: 54$ | $18: 54$ | $19: 54$ | $21: 54$ |
| Kodiang | $13: 00$ | $15: 00$ | $17: 00$ | $18: 00$ | $19: 00$ | $20: 00$ | $22: 00$ |
| Anak Bukit | $13: 13$ | $15: 13$ | $17: 13$ | $18: 13$ | $19: 13$ | $20: 13$ | $22: 13$ |
| Alor Setar | $13: 18$ | $15: 18$ | $17: 18$ | $18: 18$ | $19: 18$ | $20: 18$ | $22: 18$ |
| Kobah | $13: 29$ | $15: 29$ | $17: 29$ | $18: 29$ | $19: 29$ | $20: 29$ | $22: 29$ |
| Gurun | $13: 39$ | $15: 39$ | $17: 39$ | $18: 39$ | $19: 39$ | $20: 39$ | $22: 39$ |
| Sungai Petani | $13: 52$ | $15: 52$ | $17: 52$ | $18: 52$ | $19: 52$ | $20: 52$ | $22: 52$ |

The delay data was then successfully computed by using the current original train schedule. The first train's delay data was collected from Mohd Zulkifli and Noordin (2016). However, the delay interval for other six trains were created at random based on the relative delay time from the first train.

Table 2: New train schedule

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| STATION |  |  |  |  |  |  |  |  |
| Padang Besar | $12: 38$ | $14: 38$ | $16: 38$ | $17: 38$ | $18: 38$ | $19: 38$ | $21: 38$ |  |
| Bukit Ketri | $12: 50$ | $14: 50$ | $16: 50$ | $17: 50$ | $18: 50$ | $19: 50$ | $21: 50$ |  |
| Arau | $12: 57$ | $14: 57$ | $16: 57$ | $17: 57$ | $18: 57$ | $19: 57$ | $21: 57$ |  |
| Kodiang | $13: 03$ | $15: 03$ | $17: 03$ | $18: 03$ | $19: 03$ | $20: 03$ | $22: 03$ |  |
| Anak Bukit | $13: 16$ | $15: 16$ | $17: 16$ | $18: 16$ | $19: 16$ | $20: 16$ | $22: 16$ |  |
| Alor Setar | $13: 21$ | $15: 21$ | $17: 21$ | $18: 21$ | $19: 21$ | $20: 21$ | $22: 21$ |  |
| Kobah | $13: 32$ | $15: 32$ | $17: 32$ | $18: 32$ | $19: 32$ | $20: 32$ | $22: 32$ |  |
| Gurun | $13: 42$ | $15: 42$ | $17: 42$ | $18: 42$ | $19: 42$ | $20: 42$ | $22: 42$ |  |
| Sungai Petani | $13: 55$ | $15: 55$ | $17: 55$ | $18: 55$ | $19: 55$ | $20: 55$ | $22: 55$ |  |

Table 2 shows the new train schedules from Padang Besar to Sungai Petani. This schedule has been calculated based on overall results in Table 3 that containing the average of actual departure time and actual arrival time.

Table 3: Overall result of total train's delay

| Train | Average actual <br> departure time | Average actual <br> arrival time | Actual travel <br> time | Original <br> travel time | Total <br> delay |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2955 | $0: 02: 15$ | $0: 02: 52$ | $1: 22: 30$ | $1: 17: 00$ | $0: 05: 30$ |
| 2959 | $0: 02: 13$ | $0: 02: 47$ | $1: 22: 11$ | $1: 17: 00$ | $0: 05: 11$ |
| 2963 | $0: 02: 14$ | $0: 02: 50$ | $1: 22: 26$ | $1: 17: 00$ | $0: 05: 26$ |
| 2965 | $0: 02: 16$ | $0: 02: 51$ | $1: 22: 07$ | $1: 17: 00$ | $0: 05: 07$ |
| 2969 | $0: 02: 15$ | $0: 02: 52$ | $1: 22: 30$ | $1: 17: 00$ | $0: 05: 30$ |
| 2971 | $0: 02: 18$ | $0: 02: 56$ | $1: 22: 43$ | $1: 17: 00$ | $0: 05: 43$ |
| 2975 | $0: 02: 17$ | $0: 02: 56$ | $1: 22: 43$ | $1: 17: 00$ | $0: 05: 43$ |

## 4. Conclusions

KTM trains has experienced several difficulties including delays. This study focused on modelling the train scheduling problem as a mixed integer programming. This mixed integer programming model consists of eight constraints and the objective function is to minimize the summation of the delay experienced by all trains when it reaches their final destination. Hence, by using the model, the total delay for seven trains (Train No. 2955, 2959, 2963, 2965, 2969, 2971, and 2975) are estimated involving nine stations starting from Padang Besar to Sungai Petani. In addition, this study assumed that all trains experienced delay since the first station

The findings revealed a significant time difference between the current train schedule and anticipated journey times on all trains. Based on the estimated total delay, this study proposed a new schedule for all seven trains from Padang Besar to Sungai Petani. This new schedule will help KTM to revise their current schedule in order to reduce the waiting time of the passengers.

Table 3 shows the average of actual departure time, average of actual arrival time, actual travel time, original travel time and the total delay for every train that departure from Padang Besar to Sungai

Petani. As for trains No. 2971 and No. 2975, it recorded the highest delay time which is 5 minutes 43 seconds and followed by other trains which are No. 2955 and No. 2969 with their total delay time is 5 minutes 30 seconds, each. The least delay time for this destination belonged to train No. 2965 with recorded delay time 5 minutes and 7 seconds.

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