

UNIVERSITI TEKNOLOGI MARA

TECHNICAL REPORT

MODELLING OF THE RUBIK'S CUBE'S SOLUTION  
USING GROUP THEORY

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IN THE NAME OF ALLAH, THE MOST GRACIOUS, THE MOST MERCIFUL

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## **ABSTRACT**

Group theory is one of the area in the abstract algebra. The concept of group theory is complicated to understand and difficult to relate the real situation. The group theory have been applied into the famous toy in the century, the Rubik's cube. In this research, the group theory are explained in detailed. The researcher from mathematical computing have founded the lowest step to solve the Rubik's cube by using upper bound and lower bound. However, the solution of the Rubik's cube can be done by using the group theory. The application of the group theory in the movements of the Rubik's cube are discussed through the concept and properties of group theory in the properties of the Rubik's cube. As a result, the Rubik's cube are explained in simple way by using the group theory as the connection between them is clear and easy to understand.

# 1 INTRODUCTION

## 1.1 Research Background

According to Webster (2012), the Rubik's cube is a cube consisting of 6 sides with 9 individual pieces on each. The cube consists of 26 unique miniature cubes which are known as "cubies" or "cubelets". The cubies include a concealed inward extension that interlocks with the other cubies, while permitting them to move to different locations. However, the centre of the cube is a single square. The Rubik's cube is originally known as "Hungarian Cube" and was changed to "Magic Cube" during 1975. In 1980, the Magic cube was changed to "Rubik's Cube" by Tom Kremer.

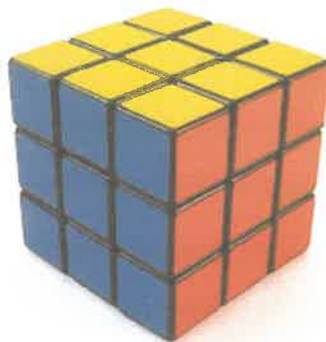


Figure 1.1: The Rubik's Cube

The Rubik's cube is named after its creator, Erno Rubik. Erno Rubik is a professor of architecture in Budapest (Hungary) and he created the Rubik's cube during 1974. He took one month to solve the Rubik's cube. He used the Rubik's cube to teach his students about spatial relationships. His aim is to engage students in science, mathematics, and problem solving at a young age.